

Double Patterning Technology Friendly Detailed Routing

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Abstract—Double patterning technology (DPT) is a most likely lithography solution for 32/22nm technology nodes as of 2008 due to the delay of Extreme Ultra Violet lithography. However, it should hurdle two challenges before being introduced to mass production, layout decomposition and overlay error. In this paper, we present the first detailed routing algorithm for DPT to improve layout decomposability and robustness against overlay error, by minimizing indecomposable wirelength and the number of stitches. Experimental results show that the proposed approach improves the quality of layout significantly in terms of decomposability and the number of stitches with 3.6x speedup, compared with a current industrial DPT design flow.

I. INTRODUCTION

To bridge the gap between current immersion lithography and again-delayed EUV lithography, double patterning technology (DPT) receives large attention from industry and is regarded as a technically and practically viable alternative to achieve high resolution for 32/22nm nodes [1], [7], [8], [11], [13], [14], [17]. The key idea of DPT is to decompose a single layout into two masks in order to increase pitch size and improve depth of focus (DOF) [9], [15]. Fig. 1 illustrates the concept of DPT. The increased pitch size brings several advantages which enables higher resolution and better printability [7]: (a) the performance of Sub-Resolution Assist Features (SRAF) and Optical Proximity Correction (OPC) algorithms will be enhanced; (b) DPT is generic to be applied for poly, metal, active, and even via layers; (c) current manufacturing infrastructures (e.g., stepper) and materials (e.g., photo-resist) can be reused without expensive modification. These advantages all make DPT as the most prominent manufacturing solution for 32/22nm nodes.

However, the deployment of DPT needs to tackle two major challenges, layout decomposition and overlay error [1], [6], [9], [15]. As shown in Fig. 1, a layout has to be decomposed (or colored differently). Unfortunately, such decomposition is not always feasible, especially for complex 2D patterns common in metal layers [1], [12], [13] owing to new spacing constraints from DPT. For indecomposable cases, a simple solution is to modify the layout, which will be highly expensive. Another solution is to split one polygon into two in order to resolve decomposition conflicts, which will introduce a stitch as shown in Fig. 2 (a). However, a stitch is highly sensitive to

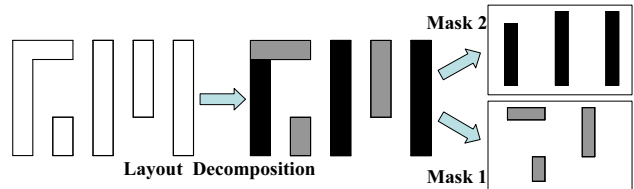
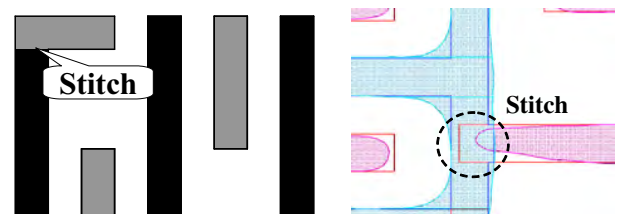


Fig. 1. In DPT, one single layer can be decomposed into two masks to effectively increase pitch size [1].

overlay error, potentially causing pinching or bridging issues as shown in Fig. 2 (b) [6], [12]. Therefore, it is important to make a layout more decomposable with fewer stitches.

There are only a few previous works on layout decomposition mainly from a mask synthesis perspective using a commercial simulator [8], design guidelines [17], and pattern matching [14]. However, all these works mainly focus on post-design optimization, which may be too late for successful decomposition. Also, none of them minimize the number of stitches systematically. Therefore, it is in great demand to take DPT into account during design time, especially detailed routing in order to generate a highly decomposable layout with a small number of stitches due to the following reasons: (a) most of hard-to-decompose patterns are from complex 2D routing wires; (b) it is the last major design optimization step with a comprehensive view on DPT; (c) there is considerable design flexibility to find reasonable tradeoff between DPT and conventional design objectives (e.g., timing, via, wirelength).

In this paper, we propose the first DPT-friendly detailed routing algorithm. The key idea behind our algorithm is to perform detailed routing and layout decomposition (or



(a) A polygon can be splitted to resolve a decomposition or coloring conflict at a cost of stitch.

(b) Stitch may result in significant printability degradation due to overlay error and line-end effect.

Fig. 2. The concept of a stitch is elaborated by an example in (a), and its susceptibility to overlay error is demonstrated in (b).

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coloring) *simultaneously* in a correct-by-construction manner to accomplish high layout decomposability and reduce the number of overlay-error-prone stitches. Therefore, our DPT-friendly detailed routing directly outputs a decomposed layout without an extra time-consuming decomposition step.

The rest of the paper is organized as follows. Section II provides preliminaries on DPT and its challenges. Section III motivates DPT consideration during design time. Then, we propose our DPT-friendly detailed routing algorithm in Section IV. Experimental results are discussed in Section V, followed by conclusion in Section VI.

II. PRELIMINARIES

A. Double Patterning Technology (DPT)

The difficulty of a process technology can be described by k_1 in Rayleigh Formulae [4], $k_1 = HP \frac{NA}{\lambda}$ where λ is wavelength of the light (currently $193nm$ for ArF lithography), NA is numerical aperture, and HP is minimum printable half-pitch. In order to print a feature in the $32nm$ node with the current single exposure infrastructure, we should increase k_1 above at least 0.25, which can be accomplished by various ways including the 3rd generation immersion fluid (Refraction Index (RI) > 1.8), larger lens, or Extreme Ultra Violet (EUV) light source ($\lambda=13.5nm$). However, in light of the physical and practical limitations in the above ways, the only feasible solution is to increase pitch size without changing minimum feature size by double patterning technology (DPT). By decomposing a layout into two masks as shown in Fig. 1, we can effectively double HP , theoretically enabling $65nm$ technology/infrastructure to print $32nm$ designs.

As expected, however, DPT process is highly complex, as one layer needs to be patterned by two exposures and two etching with two masks. There are several DPT lithography processes; litho1-etch1-litho2-etch2 (LELE) [6], spacer type DPT [2], and litho oriented DPT [16]. Although there are differences in different DPT processes, all are highly complex and involve multiple common challenges in both design and manufacturing sides such as layout decomposition and stitch minimization, which will be discussed in Section II-B.

B. Challenges in DPT

The two most important issues to deal with DPT are layout decomposition and overlay-error-prone stitches [12].

- **Layout Decomposition** in DPT is to decompose (color) the original design polygons into two groups or colors (BLACK or GRAY) to decide which polygon will be placed on which mask under the minimum double patterning spacing constraint.
- **Stitch Minimization** is another critical issue in DPT due to the overlay error which is caused by the mismatch between the first patterning and the second patterning. Unfortunately, a stitch is known to be highly sensitive to the overlay error, causing bridging or pinching. Fig. 2 (b) shows an example of a notching error due to a stitch.

Due to such criticality and importance, layout decomposition and stitch minimization have been considered during mask

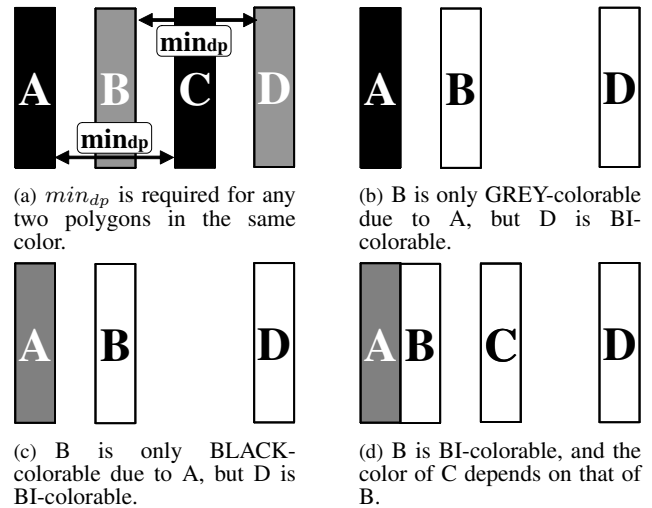


Fig. 3. This example shows the key concepts in DPT.

synthesis/manufacturing [8], [14], [17], but cannot be effectively addressed due to their high design dependency.

C. Definitions

We explain the key definitions in DPT with Fig. 3: min_{dp} , BLACK-colorable, GREY-colorable, and BI-colorable. During layout decomposition, as mentioned earlier, polygons will be divided into two masks or two colors (GREY or BLACK). And, two polygons on the same mask (thus in the same color) should maintain minimum double patterning spacing or min_{dp} . For example, since A and C are in BLACK, min_{dp} is required between two as shown in Fig. 3 (a). Such min_{dp} sometimes enforces a specific color for some polygon, if there is an already colored polygon nearby. Consider Fig. 3 (b). Since A is already in BLACK, B should be colored as GREY not to violate the min_{dp} constraint, thus B is only GREY-colorable. Similarly in Fig. 3 (c), B is only BLACK-colorable. In both Fig. 3 (b) and (c), D can be colored in either way as it has enough spacing from B, so called BI-colorable.

An interesting case is in Fig. 3 (d) where A and B are abutting. For this case, B is BI-colorable, because coloring B as GREY does not violate the min_{dp} constraint (as, A and B can be treated as one bigger polygon) and coloring B as BLACK is still fine at a cost of a stitch. The color of C depends on how B will be colored. If B is in GREY eventually, then C will be BLACK-colorable (otherwise GREY-colorable).

III. MOTIVATIONS

In this section, we illustrate the complexity of layout decomposition in Section III-A. Then, we further motivate why detailed routing can make significant impact on layout decomposition as well as the number of stitches in Section III-B.

A. Complexity of Layout Decomposition

At the first glance, layout decomposition for DPT seems identical to the phase-assignment problem [3], as both can

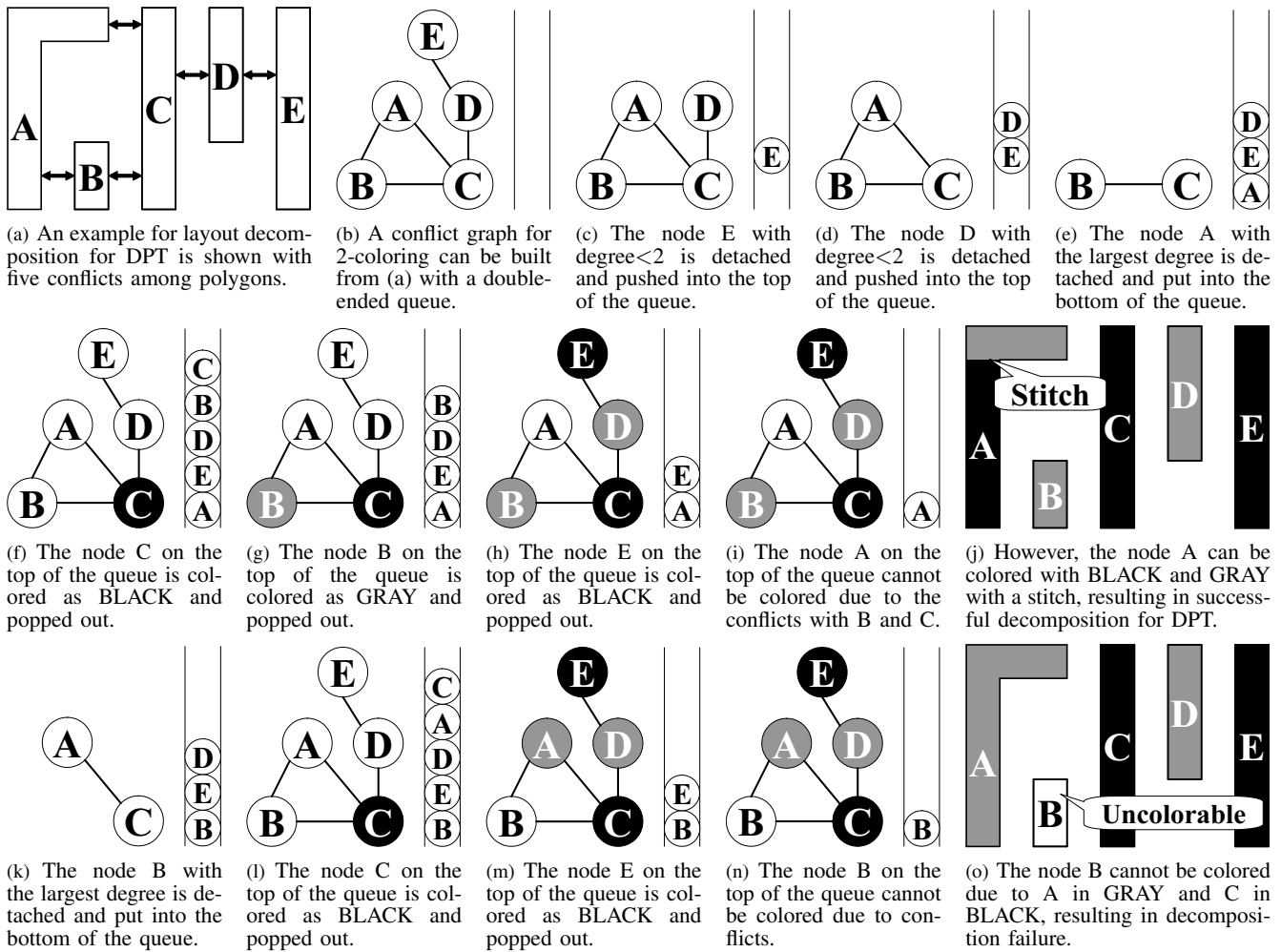


Fig. 4. This example describes a layout decomposition approach based on 2-coloring of a conflict graph in (a)–(j), but further shows that the same layout cannot be decomposed by the same 2-coloring approach as shown in (k)–(o), depending on how to spill nodes. Therefore, layout decomposition for DPT is not equivalent to but much more complex than 2-coloring, while phase-assignment is equivalent to 2-coloring [10].

be formulated as a 2-coloring problem. However, there are two key differences. Phase-assignment is for the space between polygons, but layout decomposition for DPT is for the polygons. More importantly, resolving a conflict in phase-assignment needs to involve layout modification (e.g., increasing spacing) [3], but not necessarily in DPT, as a polygon can be severed into multiple polygons without altering a layout.

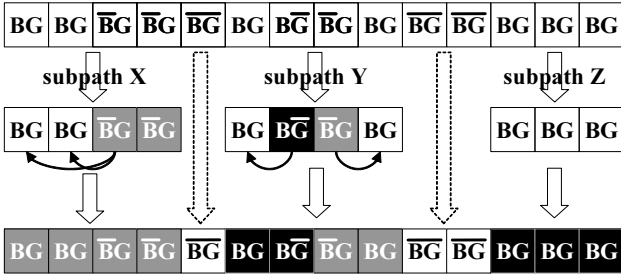
Consider a layout in Fig. 4 (a) where five disconnected polygons are shown along with five conflicts in double-headed arrows. We can formulate layout decomposition of Fig. 4 (a) as a 2-coloring problem by building a corresponding conflict graph and performing 2-coloring (BLACK or GRAY) based on Chatin’s algorithm [5]. In Fig. 4 (b), a conflict graph for the layout in (a) is constructed and a double-ended queue for coloring is prepared. As in Chatin’s algorithm, a node with degree < 2 is repeatedly detached from the graph and pushed into the top of the queue. In Fig. 4 (c), the node E is detached, which successively reduces the degree of the node D to 1, resulting in Fig. 4 (d). Since there is no node with degree 1 in Fig. 4 (d), we decide to spill the node A, thus insert to the

bottom of the queue as in Fig. 4 (e). Then, as both B and C have degree 1, we can push B, then C into the queue.

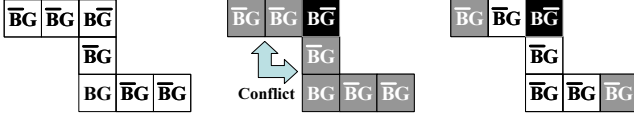
Once all the nodes are stored in the queue, we can pop out one node from the top of the queue at a time for coloring. As in Fig. 4 (f), we pop out C and color it as BLACK. Next, we can pop out B and color it as GRAY not to conflict with C as in Fig. 4 (g). After several steps including Fig. 4 (h), we encounter the situation in Fig. 4 (i) where A cannot be colored due to the conflicts with B and C. In a 2-coloring problem, such situation implies this graph is uncolorable, which requires layout modification in phase-assignment [10], but not necessarily in DPT. As in Fig. 4 (j), layout decomposition can be completed by splitting the polygon A into two parts at a cost of stitch on A.

Let us also consider the result of not selecting A in Fig. 4 (e). Although we decide to spill the node B instead of A as shown in Fig. 4 (k), it is still impossible to make the graph 2-colorable as in Fig. 4 (n). However, this will make the layout indecomposable as shown in Fig. 4 (o).

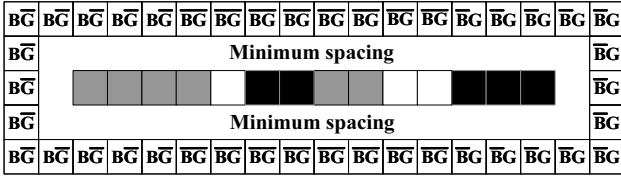
As a result, differently from the phase-assignment prob-



(a) This example shows how to color a set of grids in a routing path using Algorithm 1.



(b) This example has a potential conflict within a path. (c) A simple coloring results in a conflict around the jog. (d) Some grids become uncolored to resolve the conflict.



(e) Once the routing path is color, neighboring grids need to be shadowed by Algorithm 2.

Fig. 5. A routing path can be efficiently colored while minimizing the number of stitches, and its neighboring grids are shadowed for remaining unrouted/uncolored nets.

lem [3], the fact that a conflict graph is not 2-colorable does not guarantee the infeasibility of layout decomposition for the corresponding layout, because some conflicts can be resolved by stitches. The complexity of a layout decomposition for DPT with the minimum number of stitches is unknown yet, but we believe it is NP-hard, as there are many places for stitches.

B. DPT Consideration during Design

Layout decomposition is the most critical step for DPT, as discussed in Section II, especially in metal layers due to 2D patterns (while the poly layer has 1D patterns mostly). However, layout decomposition itself can be very complex and cannot be solved by a 2-coloring algorithm as discussed in Section III-A, which clearly requires design time consideration, more specifically during detailed routing. Current industrial effort is to first finish detailed routing, then perform layout decomposition (coloring all the polygons either in BLACK or GRAY) for DPT. If there is any uncolorable polygon, ripup/rerouting should be performed repeatedly to fix the conflict, resulting in long design-turn-around-time [6]. A detailed routing oblivious to DPT may generate highly complex patterns which may increase the uncolorable wirelength. Additionally, finding a decomposable layout is not sufficient for successful DPT processes; the number of stitches should be minimized to make a layout robust against overlay

TABLE I
GRID STATE FOR DPT COLORING

| grid state | description | grid color |
|------------------|-----------------|---------------|
| BG | BI-colorable | Nearest color |
| $B\bar{G}$ | BLACK-colorable | BLACK |
| $\bar{B}G$ | GRAY-colorable | GRAY |
| $\bar{B}\bar{G}$ | Uncolorable | No color |

error. Therefore, it is critical to consider DPT in a correct-by-construction manner during detailed routing.

IV. DPT-FRIENDLY DETAILED ROUTING

In this section, we propose our DPT-friendly detailed routing algorithm. As a first step, we propose a routing path coloring algorithm to minimize the number of stitches in Section IV-A, which provides two key observations for DPT-friendly detailed routing in Section IV-B.

A. Routing Path Coloring

For DPT-friendly detailed routing, it is critical to color a routed path with fewer stitches and shorter uncolored wirelength. Hence, we introduce a two-bit variable for each detailed routing grid to maintain colorability which will be one of the four states in Table I. As a grid with BG can be in either BLACK or GRAY, we have to find the best color for the grid in order to minimize the number of stitches.

Algorithm 1 Coloring_Path

Require: a path p

```

1: split  $p$  into a set of colorable subpaths by the  $\bar{B}\bar{G}$  state
2: for each path  $t \in S$  do
3:   for each ordered grid  $d \in t$  do
4:     if  $d.state == \bar{B}G$  then
5:       Color  $d$  as GRAY
6:     else if  $d.state == B\bar{G}$  then
7:       Color  $d$  as BLACK
8:     end if
9:   end for
10:  for each ordered grid  $d \in t$  do
11:    if  $d.state == BG$  then
12:      Color  $d$  with the nearest color
13:    end if
14:  end for
15: end for
16: for each ordered grid  $d \in p$  do
17:   for each grid  $x$  whose distance from  $d < min_{dp}$  do
18:    if  $d.state == x.state$  and both colored and any uncolored grid or stitch exists between  $d$  and  $x$  then
19:      Uncolor  $x$ 
20:    end if
21:   end for
22: end for
23: Color_Shadow( $p$ )

```

Algorithm 2 Color_Shadow

Require: A path p

```

1: for each ordered grid  $d \in p$  do
2:   for each grid  $x$  whose distance from  $d < min_{dp}$  do
3:     if  $x \notin p$  then
4:       if  $d$  is in BLACK then
5:         if  $x.state == BG$  then
6:            $x.state == \overline{BG}$ 
7:         else if  $x.state == \overline{BG}$  then
8:            $x.state == BG$ 
9:         end if
10:      else if  $d$  is in GRAY then
11:        if  $x.state == BG$  then
12:           $x.state == \overline{BG}$ 
13:        else if  $x.state == \overline{BG}$  then
14:           $x.state == BG$ 
15:        end if
16:      end if
17:    end if
18:  end for
19: end for

```

Our coloring algorithm for a routing path is proposed in Algorithm 1. To reduce the problem size, we slice a path into multiple subpaths in line 1, if there is any grid in the \overline{BG} state. Next, we color grids in either the $B\overline{G}$ or $\overline{B}G$ state, as they have a single option in lines 2–9. For remaining grids which are in the BG state, we color each one with the nearest color along the corresponding subpath in lines 10–15. Since there can be within-path conflicts, we also perform post-processing in line 16–22. Once a path is colored, we shadow around the path in line 23, which is described in Algorithm 2, to update the states of nearby grids. We visit grids which are within min_{dp} distance from the path in order to update their colorability.

Assume that a routing path with 14 uncolored grids at various states as shown in Fig. 5 (a). We begin by splitting the path into three subpaths, X, Y, and Z, as in line 1 of Algorithm 1. For each subpath, we first color grids in the $B\overline{G}$ or $\overline{B}G$ state. Then, we color remaining grids in the BG state, by identifying the nearest color within the same subpath, as shown by the arrows in Fig. 5 (a). When a subpath consists of only grids in the BG state like subpath Z, we color them randomly. Finally, we assemble subpaths and grids in the \overline{BG} state into one colored path.

For some case, there can be conflicts within a path. Consider Fig. 5 (c) where there is a jog. If we color the path in Fig. 5

TABLE II
LOOKUP TABLE FOR DPT ROUTING

| case | current grid state | next grid state | penalty |
|------|--------------------|-----------------|-----------------------|
| 1 | $B\overline{G}$ | $B\overline{G}$ | α (stitch) |
| 2 | $\overline{B}G$ | $\overline{B}G$ | α (stitch) |
| 3 | any state | \overline{BG} | β (uncolorable) |

Algorithm 3 DPT-Friendly Detailed Routing

Require: A set of blockages B , a set of nets N

```

1: layout decomposition and color shadowing of  $B$ 
2: for each net  $n \in N$  do
3:    $s$  = source grid of  $n$ 
4:    $t$  = target grid of  $n$ 
5:   A priority queue  $Q = \{s\}$ 
6:   while  $Q$  is not empty do
7:      $x$  = dequeue from  $Q$ 
8:     if  $x == t$  then
9:       break
10:    end if
11:    for each adjacent grid  $d$  of  $x$  do
12:       $cost = x.cost + 1 + A * cost$  //unit wirelength is 1
13:      if  $x.state == B\overline{G}$  and  $d.state == \overline{BG}$  then
14:         $cost += \alpha$  //to discourage a stitch
15:      else if  $x.state == \overline{B}G$  and  $d.state == B\overline{G}$  then
16:         $cost += \alpha$  //to discourage a stitch
17:      else if  $d.state == \overline{BG}$  then
18:         $cost += \beta$  //to reduce uncolorable wirelength
19:      end if
20:      if  $x$  and  $d$  not on the same layer then
21:         $cost += \gamma$  //to discourage too many vias
22:      end if
23:      if  $d.cost > cost$  then
24:         $d.cost = cost$ 
25:         $d.prev = x$ 
26:        enqueue  $d$  to  $Q$ 
27:      end if
28:    end for
29:  end while
30:   $p$  = Backtrace from  $x$  to  $s$  of  $n$ 
31:  Coloring_Path( $p$ )
32: end for

```

(b) as done in Fig. 5 (a), we will have Fig. 5 (c) where there is a conflict. Therefore, as the routing path is given and fixed, we need to detect the conflict and further resolve it by uncoloring some grids in GRAY as shown in Fig. 5 (d), which is done in lines 16–22 of Algorithm 1. Fig. 5 (e) shows the states of nearby grids after color shadowing. Note that a grid which is close to both BLACK and GREY becomes in the \overline{BG} state.

We can make two observations with the example in Fig. 5: (a) having a grid in the \overline{BG} state on a path will result in layout decomposition failure; (b) having two grids in the $B\overline{G}$ and $\overline{B}G$ states adjacent along a path will result in a stitch.

B. Detailed Routing Algorithm

According to the observations in Section IV-A, we will penalize three cases in Table II during detailed routing as shown in Algorithm 3. In line 1, we perform layout decomposition for existing routing blockages (e.g., pins, power/ground, clock, and so on) using Chatin’s algorithm [5] as done in Section III-A. When we need to spill a node, we pick one corresponding to the largest polygon. Next, we perform color shadowing

TABLE III
PERFORMANCE OF THE PROPOSED DPT-FRIENDLY DETAILED ROUTING ALGORITHM.

| design | nets | area (μm^2) | router | wirelen(mm) | | | via | router | runtime (sec) | | | double patterning | | Ratio | | |
|--------|------|-----------------------|--------|-------------|------|------|-----|--------|---------------|---------------|-----|---------------------|---------------------------------|-------|---------|--------|
| | | | | M1 | M2 | sum | | | M1-M2 | decomposition | sum | stitch ^a | failure(μm) ^b | via | runtime | stitch |
| test1 | 6K | 15K | DR+LD | 1.97 | 8.7 | 10.6 | 189 | 91.7 | 1099.6 | 1191.3 | 109 | 7.75 | 1 | 3.27 | 21.8 | |
| | | | DPFR | 1.98 | 8.7 | 10.7 | 216 | 364.6 | 0 | 364.6 | 5 | 0.15 | 1.14 | 1 | 1 | |
| test2 | 8K | 12K | DR+LD | 0.54 | 10.2 | 10.8 | 57 | 120.2 | 1517.1 | 1697.3 | 92 | 10.60 | 1 | 4.33 | 92 | |
| | | | DPFR | 0.54 | 10.2 | 10.8 | 59 | 392.9 | 0 | 392.9 | 1 | 0 | 1.04 | 1 | 1 | |

^a The number of stitches.

^b The uncolored wirelength due to irresolvable conflicts.

around the colored blockages to guide detailed routing. Then, we perform a typical detailed routing algorithm based on A* search as found in line 12. However, to find a DPT-friendly path, we modify cost from lines 13 to 22. From lines 13–16, we add α penalty to the routing cost to discourage stitches from the case 1 and 2. And, in line 18, we also increase the routing cost by β to minimize the number of uncolored grids. In line 21, we can see one more penalty term γ which is to minimize the number of vias, as decomposability or stitch count can be improved at a cost of via. Once the minimum cost path is found, we can apply Algorithm 1 as in line 31.

V. EXPERIMENTAL RESULTS

We implement our DPT-friendly routing in C++ and test on a 3.0 GHz Linux machine with 16G RAM. We scale down two industrial ASIC designs from 65nm to 32nm for evaluation.

For though comparison, we prepare two detailed routing algorithms for DPT, **DR+LD** (Detail Routing + Layout Decomposition) and **DPFR** (Double Patterning Friendly Routing). For layout decomposition in **DR+LD**, we use the same function in Algorithm 3 (See Section IV-B). We first run a grid-based detailed router followed by layout decomposition in **DR+LD** which is according to the current industrial effort [6], but layout decomposition and detailed routing are simultaneously performed by Algorithm 3 in **DPFR**.

We compare **DPFR** and **DR+LD** on four test designs with $\alpha = 9$, $\beta \gg 10$, and $\gamma = 6$ as shown in Table III, which demonstrates the effectiveness of **DPFR**, a simultaneous layout decomposition and detailed routing for DPT. With negligible overhead in wirelength, we can improve the quality of layouts in terms of double patterning; the number of stitches for every design is reduced by at least 21x and up to 92x, and the uncolorable wirelength is at most $0.15\mu m$ while **DR+LD** has at best $7.75\mu m$. Note that the uncolorable wirelength from **DPFR** is due to DPT-oblivious pin locations. Via overhead is 9% on average. Even though **DPFR** is slower than the routing portion of **DR+LD**, **DPFR** is at least 3x faster considering the overall flow. It is mainly because **DR+LD** has to work on a larger conflict graph for the final layout decomposition.

VI. CONCLUSION

Double patterning technology (DPT) is the current forerunner lithography solution for 32/22nm technology nodes, due to delayed deployment of EUV for mass production. In this paper, we present the first DPT friendly detailed routing algorithm which performs routing and layout decomposition in one

shot, in a correct-by-construction manner. Experimental results show that our approach outperforms the current industrial sequential approach (routing, and then layout decomposition) by wide margin, for both quality of results and runtime. We plan to research on DPT compatible standard cell design techniques and DPT aware placement algorithms.

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